Diagram

Free body diagram, EOM

State space representation

Cost function graph, J and B for non linear case

Tables of damping coefficient, RMS

Case 3 is the worst. Case 4 should be better